

An introduction to Model Predictive Control (MPC) for energy systems operation

Adrian Bürger^{1,2}, Angelika Altmann-Dieses¹, Gianluca Frison², Moritz Diehl²

 ¹ Institute for Refrigeration, Air-Conditioning and Environmental Engineering (IKKU), Karlsruhe University of Applied Sciences, Germany
 ² Systems Control and Optimization Laboratory, Department of Microsystems Engineering (IMTEK), University of Freiburg, Germany



Overview



- Model Predictive Control
 - General concept, advantages, and challenges
 - Advantages for energy system operation
- Problem formulations and classes
 - Formulation and solution of optimal control problems
 - Modeling and complexity
- Software and methods
 - Software frameworks and numerical solvers
- Illustrative example of MPC performance
 - One-year simulation study for a building energy system



- General concept of Model Predictive Control (MPC)
 - MPC describes a set of control methods that make explicit use of models for control of a system
 - MPC computes a sequence of control signals that are optimal for control of a system for a defined objective and time horizon
 - MPC is able to consider system dynamics, possible constraints for states and controls, and the current state of the system
 - Various fields of applications, from mechanical system to process control, and (of course) for energy system operation



• Advantages of MPC

- Suitable for systems with multiple inputs and outputs
- Intrinsic compensation of dead times
- Explicit consideration of constraints of states and controls
- Can consider future system behavior, as well as current and future references and disturbances in current control decisions

• Challenges of MPC

- Application of MPC requires prior formulation of an Optimal Control Problem (OCP) that describes system dynamics, relevant constraints and bounds sufficiently
- MPC (typically) requires solution of this OCP within real-time suitable time scales for the considered system



- Advantages of MPC for energy system operation
 - Forecasts for availability and demand of thermal and electrical energy can be directly included in predictive control decisions
 - Thermal and electric storages can be used systematically for bridging times of low energy availability and load shifting
 - Situational and individual control decisions for utilization of components and machinery can be made
 - Availability of computation time for energy systems (at least for thermal systems) is rather high

Problem formulation and classes I



• Formulation of Optimal Control Problems (OCPs)

$$\begin{array}{ll} \underset{x(\cdot),u(\cdot)}{\text{minimize}} & \int_{t_0}^{t_f} L(x(t),u(t)) \, dt + M(x(t_f)) & (1a) \\ \text{subject to} & \text{for } t \in [t_0,t_f] : \\ & \dot{x}(t) = f(x(t),u(t),c(t)) & (1b) \\ & 0 \le h(x(t),u(t),c(t)) & (1c) \\ & 0 \le r(x(t_f)) & (1d) \\ & \vec{x}(t_0) = \vec{x}_0, & (1e) \\ & \vec{x}(t) \in \mathcal{X}, \quad \vec{u}(t) \in \mathcal{U}. & (1f) \end{array}$$

$\rightarrow\,$ OCP needs to be solved within real-time suitable time scales



- Solution of optimal control problems
 - For numerical solution, OCP needs to be discretized, for which different families of methods exist:
 - Hamilton-Jacobi-Bellmann equations
 - indirect methods (first optimize, then discretize)
 - direct methods (first discretize, then optimize)
 - For larger system of practical relevance, direct methods, especially *direct multiple shooting* and *direct collocation*, are favorable
 - Depending on the characteristics of the OCP, this yields optimization problems of different complexity



- Linear vs. nonlinear problem formulations
 - Linear modeling as in, e.g.,

$$\dot{x}(t) = Ax(t) + Bu(t) \tag{2}$$

allows for linear optimization problems, which yields the possibility for global optimal and typically faster solutions of the problem

- Nonlinear modeling as in, e.g.,

$$\dot{x}(t) = f(x(t), u(t))$$
(3)

can yield improved system descriptions, however, possibly at the cost of global optimality and increased solution times of nonlinear optimization problems



- Continuous vs. discrete states and controls
 - OCPs containing purely continuous states and controls as in, e.g.,

$$x(t) \in \mathbb{R}^{n_x}, \ u(t) \in \mathbb{R}^{n_u}, \tag{4}$$

results in continuous optimization problems that can be solved rather efficiently $% \left({{{\left[{{{C_{{\rm{s}}}} \right]}}} \right)$

- OCPs where some or all states and controls only take discrete values as in, e.g.,

$$u(t) = \begin{pmatrix} u_{c}(t) \\ u_{d}(t) \end{pmatrix}, \ u(t) \in \mathbb{R}^{n_{u_{c}}}, u(t) \in \mathbb{Z}^{n_{u_{d}}}$$
(5)

result in mixed-integer optimization problems that are typically harder to solve



- Software frameworks and numerical solvers
 - A wide variety of software frameworks and numerical solvers exist, whose suitability and applicability depends various factors, such as:
 - problem class (linear, nonlinear, mixed-integer, ...)
 - structure of the optimization problem (dense, sparse, ...)
 - available computation time (microseconds, seconds, minutes, ...)
 - computation platform (PLC, microcrontroller, PC, ...)
 - One framework we often use: CasADi
 - Open-source dynamic optimization framework for discretization of OCPs and implementation of the resulting optimization problems
 - Interfaces to several simulation and optimization routines
 - Automatic generation of derivatives using Algorithmic Differentiation (AD)
 - Many useful features, such as C-Code generation and automatic setup of Spline interpolations



One-year-simulation of a building energy system¹



¹ Bürger A, Bohlayer M, Hoffmann S, Altmann-Dieses A, Braun M, Diehl M: A whole-year simulation study on nonlinear mixed-integer model predictive control for a thermal energy supply system with multi-use components. Applied Energy 258 (2020), 114064.



- Setup and results of the study²
 - Economic mixed-integer nonlinear MPC with 24 h prediction horizon using direct collocation in CasADi, IPOPT, and pycombina
 - Performance comparison to an elaborate conventional controller
 - MPC operation reduced yearly energy consumption of heat pump and heating rods by more than $18\,\%$
 - Counter-intuitive control decisions identified new use cases for system components
 - \rightarrow MPC well suited for control of the system
 - $\rightarrow\,$ Simulation study allowed to identify previously unknown, beneficial operation modes of the system

²Bürger A, Bohlayer M, Hoffmann S, Altmann-Dieses A, Braun M, Diehl M: A whole-year simulation study on nonlinear mixed-integer model predictive control for a thermal energy supply system with multi-use components. Applied Energy 258 (2020), 114064.



Thank you for your attention!

I'm looking forward to your questions

This research received funding from INTERREG V Upper Rhine, project ACA-MODES.

